

NSCC 2015

Background document on ANSYS analyses

0 Contents

<u>0</u>	<u>Contents</u>	<u>1</u>
<u>1</u>	<u>Introduction</u>	<u>2</u>
<u>2</u>	<u>Terms</u>	<u>2</u>
<u>3</u>	<u>Procedure</u>	<u>2</u>
3.1	Structures	2
3.2	Elements	3
3.3	Material	3
3.4	Damping	3
3.5	Verification	4
3.6	Time-History Analysis	4
<u>4</u>	<u>Investigated Structures</u>	<u>4</u>
<u>5</u>	<u>Cross Sections and Properties</u>	<u>4</u>
5.1	CHS properties	4
5.2	CHS 240x12	5
5.3	CHS 400x12	5
5.4	CHS 1000x12	5
<u>6</u>	<u>Models</u>	<u>6</u>
6.1	Model 1 – elastic, static	6
6.1.1	General	6
6.1.2	Horizontal stiffness	6
6.1.3	Natural frequency	7
6.1.4	Stress design	9
6.1.5	Elastic limit	9
6.1.6	Plastic design	10
<u>7</u>	<u>Constant Drive</u>	<u>10</u>
7.1	Model 1 – elastic – 5 mm	10
7.2	Model 1 – plastic – 5 mm	13
7.3	Model 1 – plastic – 50 mm	16
<u>8</u>	<u>Open Questions</u>	<u>25</u>
<u>9</u>	<u>References</u>	<u>25</u>

1 Introduction

This document reports on the structural analyses for

Knoedel/Ummenhofer: Time History Simulation in Seismic Design

to be prepared for

Nordic Steel Construction Conference 2015, Tampere, Finland, 23-25 September 2015.

This paper has been accepted under ID 166.

This study is related to previous work of Knoedel (2011), Knoedel/Hrabowski (2011, 2012) and Knoedel/Hrabowski/Ummenhofer (2014). All these are seeking to excite a structure in their most unfavourable way, which would be the natural frequency with structures of linear response.

However, with structures of non-linear response, such as plastic frames, it is not quite clear a priori, which driving frequency leads to the largest storey-drift of the structure. This is due to the well known resonance foldover of the dynamic amplification function.

In this report we produce evidence to clarify this effect.

2 Terms

peak

“first peak” is referring to the first positive local maximum of the time-displacement curve

a negative displacement corresponding to the “first peak” is the minimum after “first peak”

Amplification

largest storey drift (pos. or neg.) divided by the driving amplitude

3 Procedure

3.1 Structures

See report-11_14-03-09 for Napoli paper of Knoedel/Hrabowski/Ummenhofer (2014).

See model description below.

3.2 Elements

We used a 2-D ANSYS model with plastic BEAM23. For simplification all sections were chosen to be tubular so we can follow the structural needs without being restricted by the stepped dimensions of a profile table.

The element size was chosen in a range of 0,20 m to 0,05 m. A length of 0,20 m i.e. 20 elements for the columns and 30 elements for the waler proved to be sufficient for the present analysis.

3.3 Material

We used steel with a simplified bi-linear constitutive law with isotropic hardening.

Young's modulus with 2,1 GPa was used up to a yield limit of 235 MPa. Above that we used a straight line to the ultimate tensile stress 360 MPa at assumed 20 % strain. Thus we receive an 'engineering plastic modulus' with a slope of

$$(360 \text{ MPa} - 235 \text{ MPa}) / 0,20 = 625 \text{ MPa}$$

This approach has been used before, see eq. 15 in Knoedel/Hrabowski (2012).

3.4 Damping

A parameter DAMP = 0,00235 was used to get

time [s]	displacement [mm]	description
0,818	196,2	first peak
18,803	167,4	12. peak

According to the Mensinger Formula

$$\delta = 1/N * \ln (\text{Amp}_{,i} / \text{Amp}_{,i+N})$$

the logarithmic decrement amounts to

$$\delta = 1/11 * \ln (196,2 \text{ mm} / 167,2 \text{ mm}) = 0,015$$

The damping ratio (Lehrsches Dämpfungsmaß D , critical damping ratio ζ) amounts to

$$D = \delta / 2\pi$$

$$D = 0,015 / 2\pi = 0,00239$$

3.5 Verification

See report-11_14-03-09 for Napoli paper of Knoedel/Hrabowski/Ummenhofer (2014).

See below for the individual models.

3.6 Time-History Analysis

We performed a straight forward Euler-type time integration, using 20 to 50 load steps within a period. Between these major steps automatic time stepping was used, which resulted in up to 100 sub steps in between.

20 load steps proved to be sufficient for a period within 1,2 % of the theoretical value.

Results are given in absolute values in the original coordinate system.

This can be seen from the calculations with a step base displacement, where the response-position of the base nodes is shown as offset and the dynamic response of the structure is seen as oscillation around an offset as well.

4 Investigated Structures

Frame with $w/h = 6 \text{ m} / 4 \text{ m}$ and pinned column bases.

Tubular section chs 400x12.

5 Cross Sections and Properties

5.1 CHS properties

Stiffness of the tubes

$$I = \pi * R^3 * T$$

$$R = (D - T)/2$$

$$A = 2\pi * R * T$$

5.2 CHS 240x12

$$R = (24 \text{ cm} - 1,2 \text{ cm})/2 = 11,4 \text{ cm}$$

$$I = \pi * (11,4 \text{ cm})^3 * 1,2 \text{ cm} = 5585 \text{ cm}^4$$

$$W = 5585 \text{ cm}^4 / 11,4 \text{ cm} = 490 \text{ cm}^3$$

$$A = 2\pi * 11,4 \text{ cm} * 1,2 \text{ cm} = 85,6 \text{ cm}^2$$

For information:

HEA 240:

$$I = 7760 \text{ cm}^4$$

$$W = 645 \text{ cm}^3$$

$$N_{R,k} = 85,6 \text{ cm}^2 * 235 \text{ N/mm}^2 = 2010 \text{ kN}$$

$$M_{gr,el} = 490 \text{ cm}^3 * 235 \text{ N/mm}^2 = 115,2 \text{ kNm}$$

5.3 CHS 400x12

CHS 400x12

$$R = (40 \text{ cm} - 1,2 \text{ cm})/2 = 19,4 \text{ cm}$$

$$I = \pi * (19,4 \text{ cm})^3 * 1,2 \text{ cm} = 27500 \text{ cm}^4$$

$$W = 27500 \text{ cm}^4 / 19,4 \text{ cm} = 1420 \text{ cm}^3$$

$$A = 2\pi * 19,4 \text{ cm} * 1,2 \text{ cm} = 146,3 \text{ cm}^2$$

$$N_{R,k} = 146 \text{ cm}^2 * 235 \text{ N/mm}^2 = 3430 \text{ kN}$$

$$M_{gr,el} = 1420 \text{ cm}^3 * 235 \text{ N/mm}^2 = 333,7 \text{ kNm}$$

5.4 CHS 1000x12

$$R = (100 \text{ cm} - 1,2 \text{ cm})/2 = 49,4 \text{ cm}$$

$$I = \pi * (49,4 \text{ cm})^3 * 1,2 \text{ cm} = 454500 \text{ cm}^4$$

(80 times bigger than 240x12)

$$W = 454500 \text{ cm}^4 / 49,4 \text{ cm} = 9200 \text{ cm}^3$$

(19 times bigger than 240x12)

$$A = 2\pi * 49,4 \text{ cm} * 1,2 \text{ cm} = 372 \text{ cm}^2$$

$$N_{R,k} = 372 \text{ cm}^2 * 235 \text{ N/mm}^2 = 8742 \text{ kN}$$

$$M_{gr,el} = 9200 \text{ cm}^3 * 235 \text{ N/mm}^2 = 2162 \text{ kNm}$$

6 Models

6.1 Model 1 – elastic, static

6.1.1 General

single storey

6 m frame width

4 m frame height

element divisor 1 m / 5

steel elastic

no density

0,00235 damping constant

1000x12 tubular waler

240x12 tubular columns

36.000 kgs mass added in each of the frame's corners

dx,dy boundary conditions: feet displacements blocked

9,81 m/s² gravity loads

6.1.2 Horizontal stiffness

1.e+06 horizontal load in left corner

919,96 mm = 920 mm associated horizontal displacement (storey-drift)

919,96 mm with EFAK 20

reduces to 911,49 with waler 5000x12

stiffness:

$$c = 1.e+06 \text{ N} / 919,96 \text{ mm} = 1087 \text{ N/mm} = 1,09*10^6 \text{ N/m}$$

calculatory horizontal displacement with infinitely stiff waler

$$c = 2 * 3 * EI / L^3$$

$$c = 2 * 3 * 2,1 * 10^5 \text{ N/mm}^2 * 5585 \text{ cm}^4 / (4 \text{ m})^3 = 1100 \text{ N/mm} = 1,10 * 10^6 \text{ N/m}$$

$$u = F / c$$

$$u = 1.e+06 \text{ N} / 1,10 * 10^6 \text{ N/m} = 909 \text{ mm}$$

seems OK for engineering purposes

6.1.3 Natural frequency

time history decay calculation

calculatory natural frequency – with theoretical stiffness

$$\omega = \sqrt{(c/m)}$$

$$\omega = \sqrt{(1,10 * 10^6 \text{ N/m} / 72000 \text{ kgs})} = 3,91 \text{ rad/s}$$

$$f = \omega / 2\pi$$

$$f = 3,91 \text{ rad/s} / 2\pi = 0,622 \text{ /s}$$

$$T = 1 / 0,622 \text{ /s} = 1,607 \text{ s}$$

calculatory natural frequency – with model stiffness

$$\omega = \sqrt{(c/m)}$$

$$\omega = \sqrt{(1,09 * 10^6 \text{ N/m} / 72000 \text{ kgs})} = 3,89 \text{ rad/s}$$

$$f = \omega / 2\pi$$

$$f = 3,89 \text{ rad/s} / 2\pi = 0,619 \text{ /s}$$

$$T = 1 / 0,619 \text{ /s} = 1,615 \text{ s}$$

(without detuning due to damping)

Numerical results for 20 increments per period and a given period of 1,673 with EFAK = 5

11 periods with peak values (first/last) 0,8365 s / 18,821 s

$$T_{\text{single,mean}} = (18,821 \text{ s} - 0,837 \text{ s}) / 11 = 1,635 \text{ s}$$

Model period is longer – compared to model stiffness – by a factor of

$$k = 1,635 \text{ s} / 1,615 \text{ s} = 1,012$$

Numerical results for 20 increments per period and a given period of 1,635 with EFAK = 5
(triggering period adjusted)

11 periods with peak values (first/last) 0,8175 s / 18,803 s

$T_{\text{single,mean}} = (18,803 \text{ s} - 0,818 \text{ s}) / 11 = 1,635 \text{ s}$

Model period is longer – compared to model stiffness – by a factor of

$k = 1,635 \text{ s} / 1,615 \text{ s} = 1,012$

(no change)

Numerical results for 50 increments per period and a given period of 1,635 with EFAK = 5
(smaller time steps, same elements)

11 periods with peak values (first/last) 0,8175 s / 18,639 s

$T_{\text{single,mean}} = (18,639 \text{ s} - 0,818 \text{ s}) / 11 = 1,620 \text{ s}$

Model period is longer – compared to model stiffness – by a factor of

$k = 1,620 \text{ s} / 1,615 \text{ s} = 1,003$

(smaller period, more accurate)

Numerical results for 20 increments per period and a given period of 1,635 with EFAK = 20
(smaller time steps, same elements)

11 periods with peak values (first/last) 0,8175 s / 18,639 s

$T_{\text{single,mean}} = (18,803 \text{ s} - 0,818 \text{ s}) / 11 = 1,635 \text{ s}$

Model period is longer – compared to model stiffness – by a factor of

$k = 1,635 \text{ s} / 1,615 \text{ s} = 1,012$

(same as EFAK = 5 and ninc = 20)

Numerical results for 50 increments per period and a given period of 1,635 with EFAK = 20
(smaller time steps, smaller elements)

11 periods with peak values (first/last) 0,8175 s / 18,639 s

$T_{\text{single,mean}} = (18,639 \text{ s} - 0,818 \text{ s}) / 11 = 1,620 \text{ s}$

Model period is longer – compared to model stiffness – by a factor of

$k = 1,620 \text{ s} / 1,615 \text{ s} = 1,003$

(smaller period, more accurate)

conclusion:

1 % error in the period seems to be ok for engineering purposes

EFAK = 5 and NINC = 20 are used throughout

6.1.4 Stress design

Horizontal force in/at waler

$$F = 100 \text{ kN}$$

Base shear per column

$$F = 50 \text{ kN}$$

Corner moment

$$M = 50 \text{ kN} * 4 \text{ m} = 200 \text{ kNm}$$

outer fibre stress

$$\sigma = 200 \text{ kNm} / 490 \text{ cm}^3 = 408 \text{ N/mm}^2$$

$$(\text{in waler: } 200 \text{ kNm} / 9200 \text{ cm}^3 = 21,7 \text{ N/mm}^2)$$

Normal forces in columns from tilting

$$F = 100 \text{ kN} * 4 \text{ m} / 6 \text{ m} = \pm 66,67 \text{ kN}$$

Normal force in waler, depending on position of horizontal force: $\pm 50 \text{ kN}$

Numerical results:

66,67 kN	normal force	ok
50,00 kN	shear	ok
200,0 kNm	moment	ok
$0,416 * 10^9 \text{ Pa} = 416 \text{ MPa}$	max sigma	rel. err. +2,0 %
$-0,416 * 10^9 \text{ Pa} = -416 \text{ MPa}$	max sigma	rel. err. +2,0 %

6.1.5 Elastic limit

Horizontal force:

$$F = 100 \text{ kN} * 235 \text{ N/mm}^2 / 408 \text{ N/mm}^2 = 57,60 \text{ kN}$$

Horizontal displacement with model stiffness:

$$w = 57,60 \text{ kN} / 1,09 \cdot 10^6 \text{ N/m} = 52,3 \text{ mm}$$

Numerical results with horizontal load 57,6 kN:

$$w = 52,99 \text{ mm} \quad \text{rel. err. } +1,3 \%$$

$$\sigma = 240 \text{ N/mm}^2 \quad \text{rel. err. } +2,1 \%$$

6.1.6 Plastic design

Numerical results with horizontal load 57,6 kN (elastic limit load):

$$w = 53,0 \text{ mm} \quad \text{plausible}$$

$$\sigma = 235 \text{ N/mm}^2 \quad \text{ok}$$

$$\epsilon_{pl} = 0,312 \cdot 10^{-4} \text{ corresponds to } 6,6 \text{ N/mm}^2 - \text{plausible}$$

left corner only, right shows no plastic strains

Numerical results with horizontal load 65 kN (little above half to fully plastic):

$$w = 61,9 \text{ mm} \quad \text{plausible}$$

$$\sigma = 235 \text{ N/mm}^2 \quad \text{ok}$$

$$\epsilon_{pl} = 0,444 \cdot 10^{-3} \quad \text{corresponds to } 93 \text{ N/mm}^2;$$

$$235 + 93 = 328 \text{ N/mm}^2 \quad \text{plausible, must be over } 270 \text{ N/mm}^2$$

$$0,5 \cdot 65 \text{ kN} \cdot 4 \text{ m} / 490 \text{ cm}^3 = 265,3 \text{ N/mm}^2$$

Counter check – 65 kN with linear material:

$$w = 59,8 \text{ mm} \quad \text{plausible}$$

$$\sigma = 270 \text{ N/mm}^2 \quad \text{rel. err. } +1,8 \%$$

7 Constant Drive

7.1 Model 1 – elastic – 5 mm

Driving period 1,635 s at resonance, driving amplitude 5 mm.

Calculatory amplitude for $\delta = 0,015$:

$$A_{\text{steady}} = A_{\text{drive}} \cdot \pi / \delta$$

$$A_{\text{steady}} = 5 \text{ mm} \cdot \pi / 0,015 = 5 \text{ mm} \cdot 209,4 = 1047 \text{ mm}$$

Numerical results with driving period 1,635, EFAK = 5 and NINC = 20
after 100 sec; 1223 load steps; 61 periods: +399 mm/–389 mm

Numerical results with driving period 1,635, EFAK = 5 and NINC = 50
after 200 sec; 6116 load steps, 122 periods:
max at 60 seconds +284 mm / –284 mm, after that decaying to +228 mm/–229 mm

Numerical results with driving period 1,635, EFAK = 5 and NINC = 40
after 100 sec; 2446 load steps, 61 periods:
max at 66 seconds +294 mm / –294 mm, after that decaying to +279 mm/–279 mm

Numerical results with driving period 1,635, EFAK = 5 and NINC = 30
after 80 sec; 1467 load steps, 48 periods:
max at 80 seconds +319 mm/–319 mm

Numerical results with driving period 1,635, EFAK = 5 and NINC = 30
after 100 sec; 1834 load steps, 61 periods:
max at 83 seconds +320 mm/–320 mm, after that decaying to +315 mm / –315 mm

Numerical results with driving period 1,635, EFAK = 5 and NINC = 20
after 200 sec; 2446 load steps, 122 periods:
max at 200 seconds +413 mm/–413 mm

Numerical results with driving period 1,635, EFAK = 5 and NINC = 20
after 300 sec; 3669 load steps, 183 periods:
max at 190-220 seconds +413 mm/–413 mm, after that decaying to +411 mm / –411 mm
at 150 seconds +410 mm/–411 mm – 99 %;
at 120 seconds +402 mm/–403 mm – 97 %;
at 100 seconds +390 mm/–390 mm – 94 %;
at 90 seconds +380 mm/–380 mm – 92 %;

Numerical results with driving period 1,635*0,9, EFAK = 5 and NINC = 20
after 200 sec; 2718 load steps, 135 periods:
max at 6,9 seconds +42,4 mm/–42,7 mm (5. peak), after that beating occurs with decaying amplitudes;
at 191 seconds +21,4 mm/–21,4 mm

Numerical results with driving period $1,635 \cdot 0,95$, EFAK = 5 and NINC = 20

after 200 sec; 2575 load steps, 128 periods:

max at 15 seconds +85,5 mm/–85,2 mm (10. peak), after that beating occurs with decaying amplitudes;

at 184 seconds +49,7 mm/–49,7 mm

Numerical results with driving period $1,635 \cdot 0,98$, EFAK = 5 and NINC = 20

after 200 sec; 2496 load steps, 124 periods:

max at 42 seconds +191 mm/–191 mm (26-27. peak), after that beating occurs with decaying amplitudes;

within 200 sec one other beating maximum occurs at 134 seconds +143 mm/–143 mm

Numerical results with driving period $1,635 \cdot 0,99$, EFAK = 5 and NINC = 20

after 200 sec; 2471 load steps, 123 periods:

max at 90 seconds +311 mm/–311 mm, after that beating occurs with decaying amplitudes;

Numerical results with driving period $1,635 \cdot 0,992$, EFAK = 5 and NINC = 20

after 200 sec; 2466 load steps, 123 periods:

max at 110 seconds +355 mm/–355 mm; after that decaying amplitudes;

Numerical results with driving period $1,635 \cdot 0,995$, EFAK = 5 and NINC = 20

after 200 sec; 2471 load steps, 123 periods:

max at 90 seconds +432 mm/–432 mm

Numerical results with driving period $1,635 \cdot 0,997$, EFAK = 5 and NINC = 20

after 300 sec; 3680 load steps, 184 periods:

max at 300 seconds +465 mm/–465 mm

Numerical results with driving period $1,635 \cdot 0,997$, EFAK = 5 and NINC = 20

after 500 sec; 6134 load steps, 306 periods:

at 50 seconds +297 mm/–299 mm – 64 %

at 100 seconds +406 mm/–407 mm – 87 %

at 150 seconds +445 mm/–445 mm – 95 % ... 92 peaks – sufficient for engineering purposes

at 199 seconds +458 mm/–458 mm – 98 % ... 122 peaks – selected for this paper

at 250 seconds +463 mm/–463 mm – 99,4 %

at 300 seconds +465 mm/–465 mm – 99,8 %

at 349 seconds +466 mm/–465 mm – 99,8 %

at 400 seconds +466 mm/–466 mm – 100 %

at 450 seconds +466 mm/–466 mm – 100 %

at 500 seconds +466 mm/–466 mm – 100 %

Numerical results with driving period 1,635*1,005, EFAK = 5 and NINC = 20

after 150 sec; 1825 load steps, 91 periods:

max at 82 seconds +304 mm/–304 mm

Numerical results with driving period 1,635*1,01, EFAK = 5 and NINC = 20

after 100 sec; 1211 load steps, 60 periods:

max at 52 seconds +235 mm/–235 mm

Numerical results with driving period 1,635*1,02, EFAK = 5 and NINC = 20

after 100 sec; 1199 load steps, 59 periods:

max at 32+33 seconds +162 mm/–162 mm (20-21. peak), after that beating occurs with decaying amplitudes;

Numerical results with driving period 1,635*1,05, EFAK = 5 and NINC = 20

after 50 sec; 582 load steps, 29 periods:

max at 14 seconds +84,6 mm/–84,7 mm (9. peak), after that beating occurs with decaying amplitudes;

Numerical results with driving period 1,635*1,1, EFAK = 5 and NINC = 20

after 50 sec; 556 load steps, 27 periods:

max at 9 seconds +48,7 mm/–49,0 mm (6. peak), after that beating occurs with decaying amplitudes;

7.2 Model 1 – plastic – 5 mm

Driving period 1,635 s at resonance, driving amplitude 5 mm.

Plastic constitutive law as described above with $f_y = 235 \text{ N/mm}^2$

Elastic limit storey-drift $w = 52,3 \text{ mm}$

Numerical results with driving period $1,635 \cdot 1,00$, EFAK = 5 and NINC = 20

after 20 sec; 244 load steps, 12 periods:

max at 9 seconds +66,1 mm/–66,2 mm (6. peak), after that steady state with constant amplitudes;

Numerical results with driving period $1,635 \cdot 1,00$, EFAK = 5 and NINC = 40

after 40 sec; 978 load steps, 24 periods:

6. peak with +66,1 mm/–66,4 mm

after 34 seconds there are some amplitudes around 68 mm, such as 68,5 mm/–68,3 mm; but this seems to be some “aliasing” rather than a steady increase of the response amplitudes.

conclusion: NINC = 40 does not lead to significant improve

Numerical results with driving period $1,635 \cdot 1,00$, EFAK = 20 and NINC = 20

after 15 sec; 183 load steps, 9 periods:

5. peak with +63,9 mm/–65,6 mm

6. peak with +65,6 mm/–65,9 mm (loadstep 110, substep 10)

7. peak with +66,2 mm/–66,1 mm

8. peak with +65,8 mm/–65,9 mm

9. peak with +66,1 mm/–66,1 mm

conclusion: EFAK = 20 does not improve significantly

Numerical results with driving period $1,635 \cdot 1,00$, EFAK = 20 and NINC = 20

after 200 sec; 2446 load steps, 122 periods:

see previous run – it is in fact steadily increasing up to 79,6 mm (loadstep 2430, substep 10) in the last period.

Numerical results with driving period $1,635 \cdot 0,90$, EFAK = 20 and NINC = 20

after 20 sec; 271 load steps, 13 periods:

max at 6. peak with +46,0 mm/–45,3 mm;

after that pronounced beating with smallest amplitudes around 5 mm

this run is purely elastic, since the limit drift is some 53 mm

Numerical results with driving period $1,635 \cdot 0,95$, EFAK = 20 and NINC = 20

after 20 sec; 257 load steps, 12 periods:

max at 5. peak with +59,2 mm/–60,3 mm; after that decaying amplitudes

12. peak with +55,1 mm/–54,7 mm

Numerical results with driving period $1,635 \cdot 0,98$, EFAK = 20 and NINC = 20

after 20 sec; 249 load steps, 12 periods:

max at 6. peak with +64,0 mm/–64,0 mm; after that decaying amplitudes

12. peak with +62,6 mm/–62,1 mm

Numerical results with driving period $1,635 \cdot 0,99$, EFAK = 20 and NINC = 20

after 20 sec; 247 load steps, 12 periods:

max at 6. peak with +65,4 mm/–65,3 mm; after that slightly decaying amplitudes

12. peak with +64,4 mm/–64,2 mm

Numerical results with driving period $1,635 \cdot 1,003$, EFAK = 20 and NINC = 20

after 100 sec; 1219 load steps, 60 periods:

6. peak with +66,0 mm/–66,4 mm – 90 % of value at 60. peak

10. peak with +66,4 mm/–66,3 mm

20. peak with +67,3 mm/–67,6 mm

30. peak with +68,9 mm/–69,2 mm

40. peak with +70,5 mm/–70,8 mm

50. peak with +72,1 mm/–71,8 mm

60. peak with +73,3 mm/–73,6 mm

61. peak with +73,5 mm/–73,7 mm

Numerical results with driving period $1,635 \cdot 1,003$, EFAK = 20 and NINC = 20

after 200 sec; 2439 load steps, 121 periods:

last peak (122.) +79,8 mm/–80,1 mm – seems as if the amplitudes were steadily increasing

Numerical results with driving period $1,635 \cdot 1,005$, EFAK = 20 and NINC = 20

after 50 sec; 608 load steps, 30 periods:

6. peak with +66,1 mm/–66,5 mm – 95 % of value at 30. peak

10. peak with +66,5 mm/–66,9 mm

15. peak with +67,4 mm/–67,5 mm

20. peak with +67,5 mm/–67,9 mm

25. peak with +68,6 mm/–68,7 mm

30. peak with +68,9 mm/–69,7 mm

Numerical results with driving period $1,635 \cdot 1,01$, EFAK = 20 and NINC = 20

after 20 sec; 242 load steps, 12 periods:

max at 6. peak with +66,2 mm/–66,3 mm; after that slightly decaying amplitudes (? see end values)

12. peak with +67,3 mm/–67,0 mm

Numerical results with driving period $1,635 \cdot 1,01$, EFAK = 20 and NINC = 20

after 40 sec; 484 load steps, 24 periods:

see previous run

24. peak with +68,8 mm/–68,5 mm

Numerical results with driving period $1,635 \cdot 1,02$, EFAK = 20 and NINC = 20

after 20 sec; 239 load steps, 11 periods:

max at 6. peak with +66,6 mm/–66,4 mm; after that like a plateau

12. peak (bottom is still visible) with +67,3 mm/–67,7 mm

Numerical results with driving period $1,635 \cdot 1,05$, EFAK = 20 and NINC = 20

after 20 sec; 232 load steps, 11 periods:

max at 6. peak with +64,1 mm/–64,4 mm; after that decaying amplitudes to 57 mm

Numerical results with driving period $1,635 \cdot 1,10$, EFAK = 20 and NINC = 20

after 20 sec; 222 load steps, 11 periods:

max at 5. peak with +46,1 mm/–45,5 mm; after pronounced beating with amplitudes down to –9 mm/+11 mm.

7.3 Model 1 – plastic – 50 mm

Driving period 1,635 s at resonance, driving amplitude 5 mm.

Plastic constitutive law as described above with $f_y = 235 \text{ N/mm}^2$

Elastic limit storey-drift $w = 52,3 \text{ mm}$

Numerical results with driving period $1,635 \cdot 1,00$, EFAK = 10 and NINC = 200

(seemed to be necessary to get the thing going over the first or second peak)

after 10 sec; 1224 load steps, 6 periods, 96269 cumulative iterations, app. 90 min I/O

1. peak; 0,81 sec; +78,6 mm / –102,3 mm (1,6922 s, loadstep208, substep 78)

2. peak; 2,5 sec; +65,6 mm / –97,4 mm

3. peak; 4,2 sec; +63,9 mm / –99,0 mm

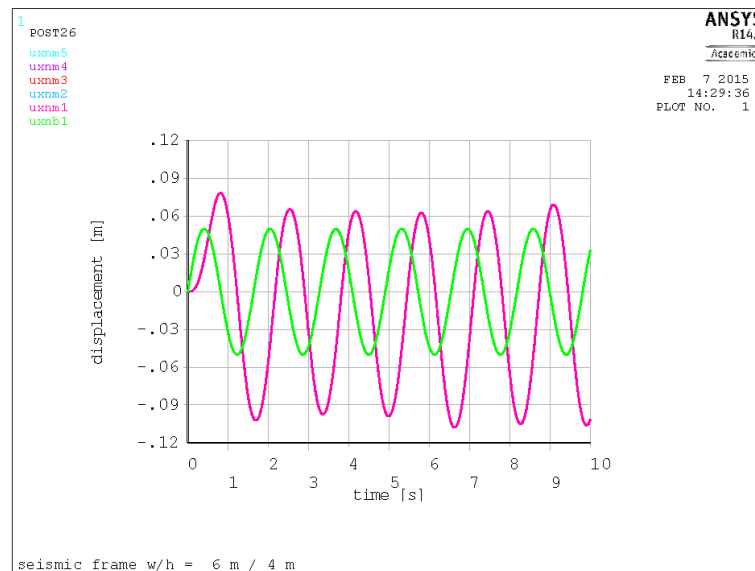
4. peak; 5,8 sec; +62,8 mm / –107,9 mm

5. peak; 7,4 sec; +64,0 mm / –105,0 mm

6. peak; 9,1 sec; +69,3 mm / –106,2 mm (9,9081 s, loadstep 1213, substep 64)

remark: up to 105 substeps were needed

remark 2: are the results of this run significant?

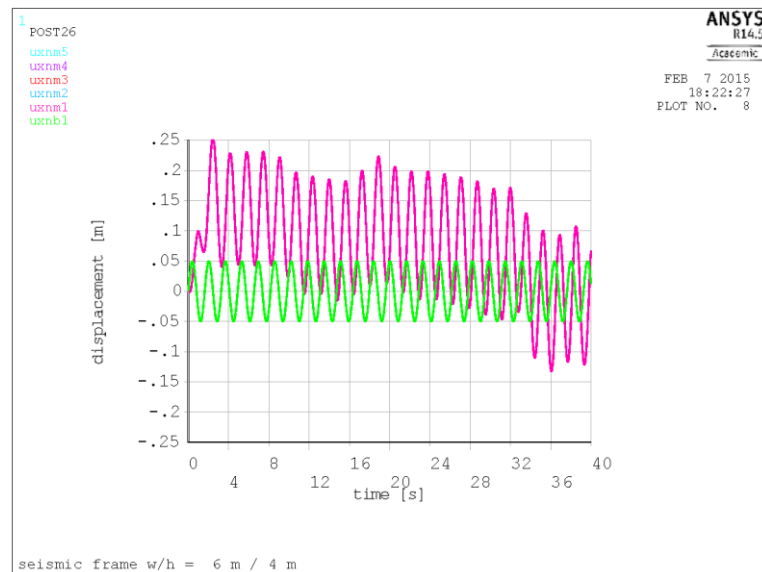


Second run with the quicker response due to use of NSUB,100,10000,10,1

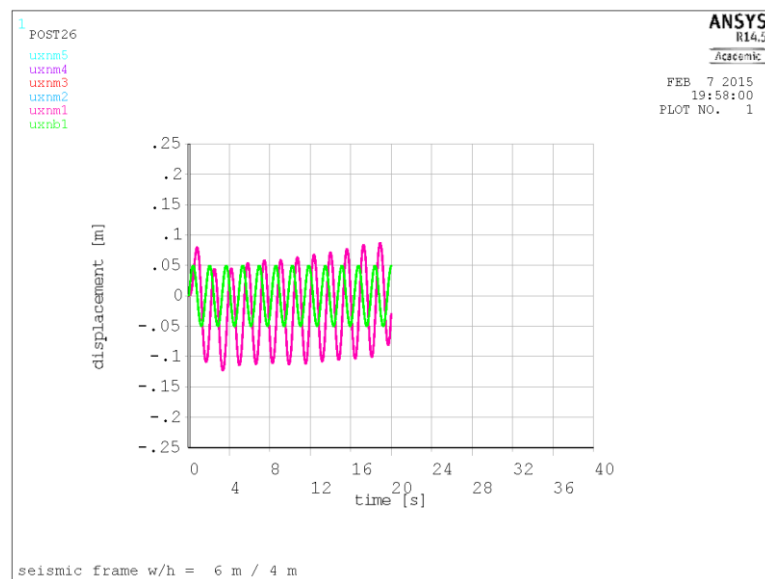
Numerical results with driving period $1,635 \cdot 1,00$, EFAK = 5 and NINC = 100

after 40 sec; 2447 load steps, 24 periods, 147311 cumulative iterations, app. 60 min I/O

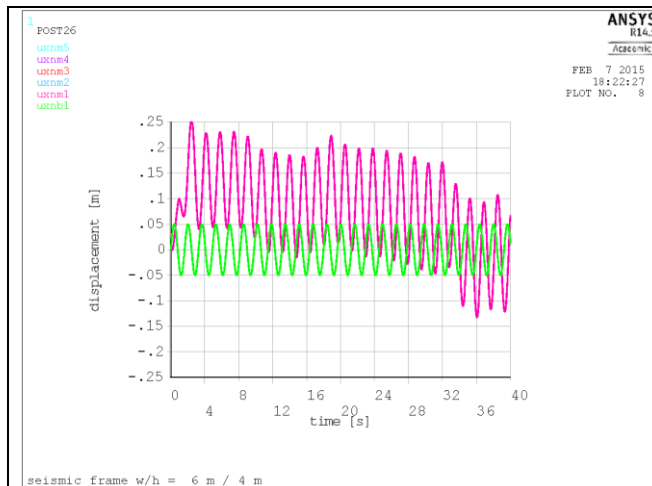
...quite different feature



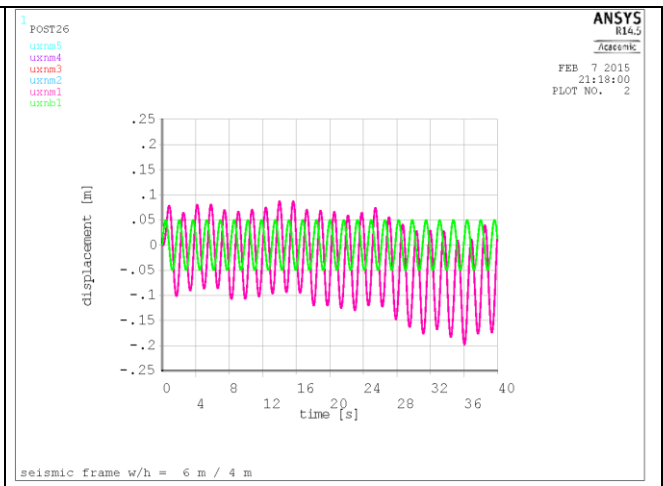
same as above, but with NINC = 200 and up to 20 sec



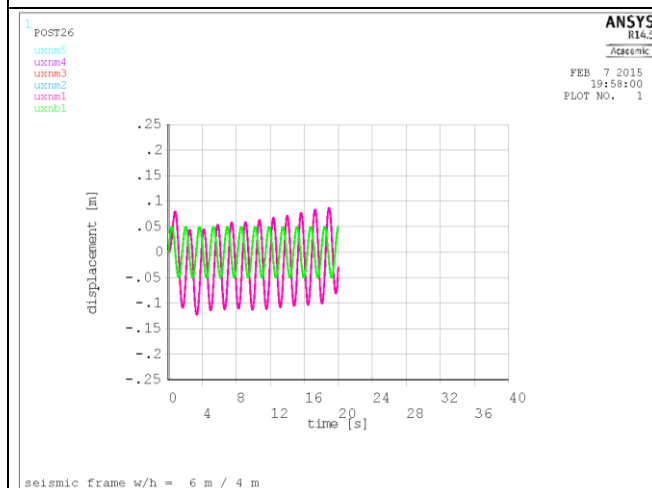
max at 3,3 sec –123 mm



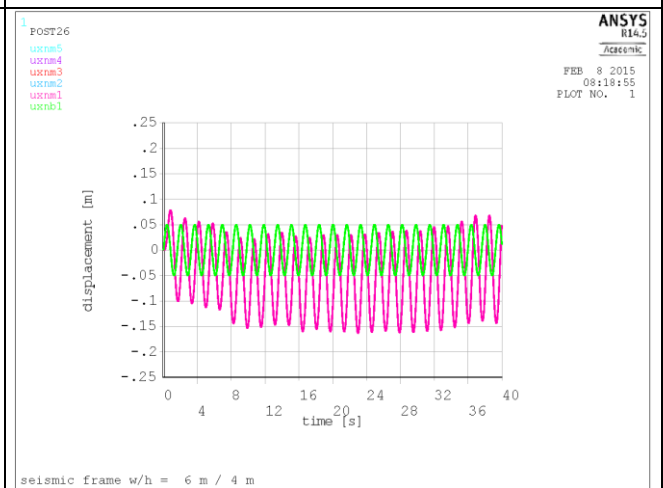
NINC = 100



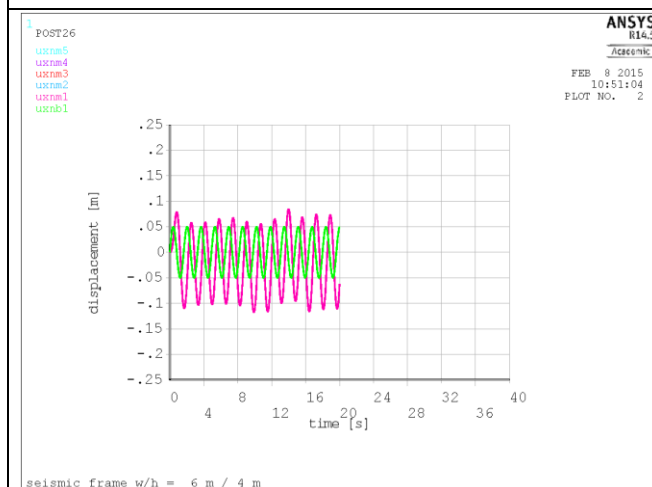
NINC = 150



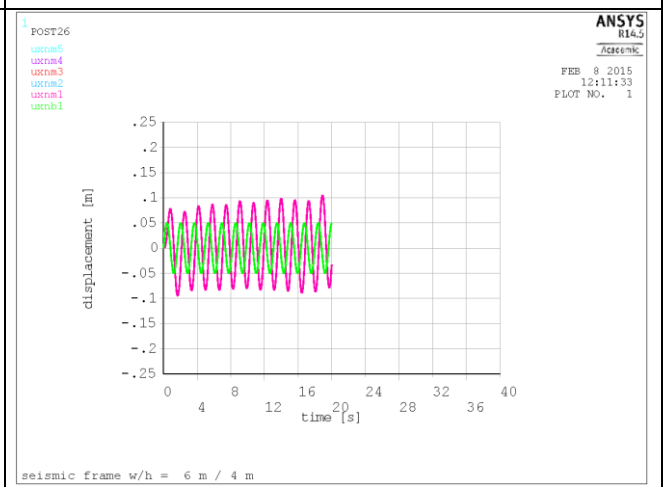
NINC = 200



NINC = 250



NINC = 300



NINC = 350

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Numerical results with driving period $1,635 \cdot 0,995$, EFAK = 5 and NINC = 100

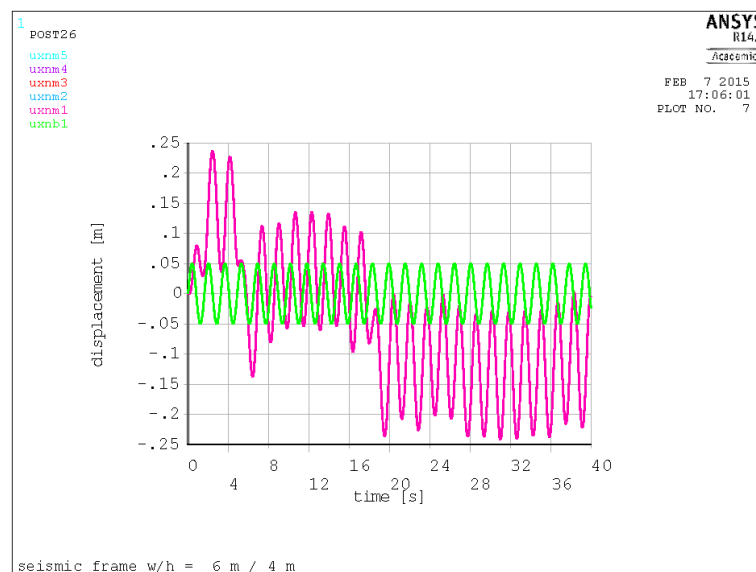
(seemed to be necessary to get the thing going over the first or second peak)

after 40 sec; 2458 load steps, 24 periods, 149896 cumulative iterations, app. 60 min I/O

max pos: 2. peak; 2,4 sec, +236,8 mm / -36,7 mm (!)

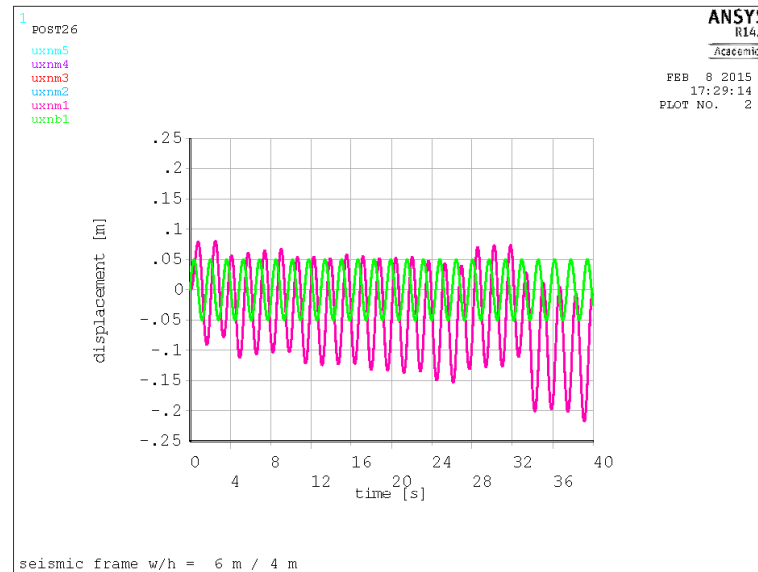
min neg: 19. peak; 30,2 sec -27,9 mm / -241,5 mm (!)

is seems that detuning which causes beating with elastic oscillators, causes a jump in the mean displacement: from app. 120 mm to app. 50 mm to app. -110 mm.

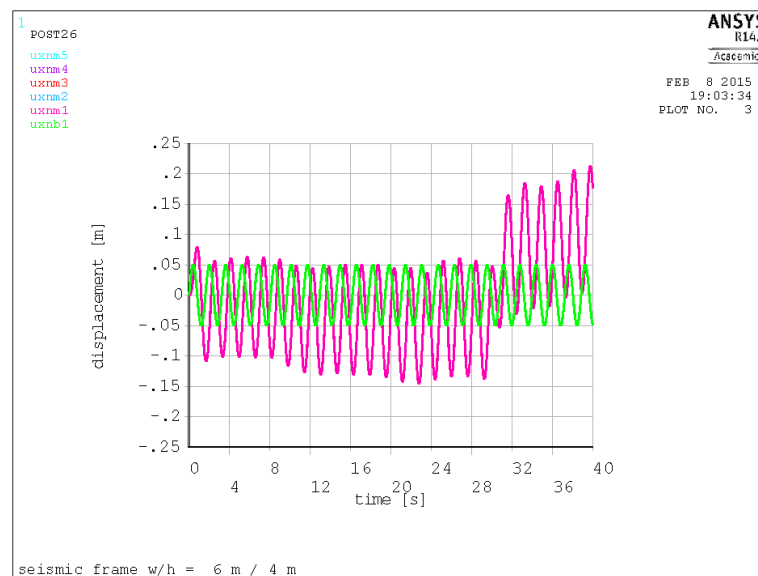


(compare run below with NINC = 200, otherwise identical)

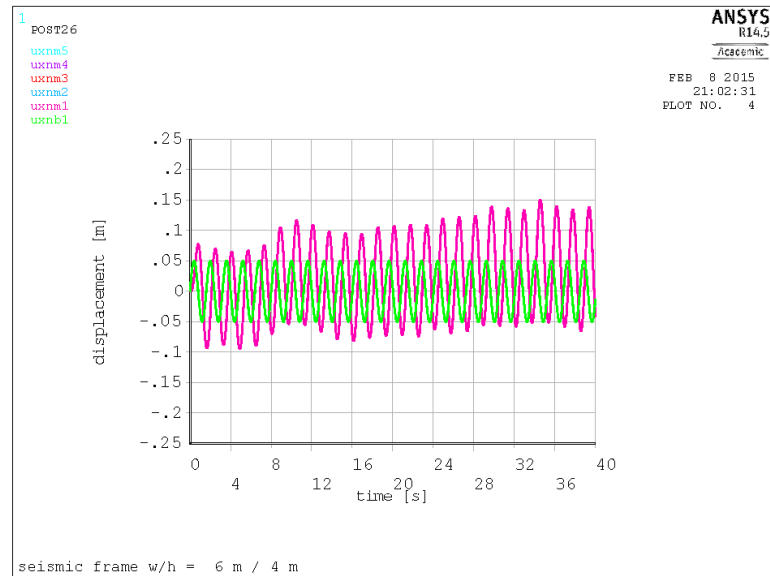
As a result of the above “6 pix on one page” page we decided that NINC = 200 would be a compromise for reasonable results.



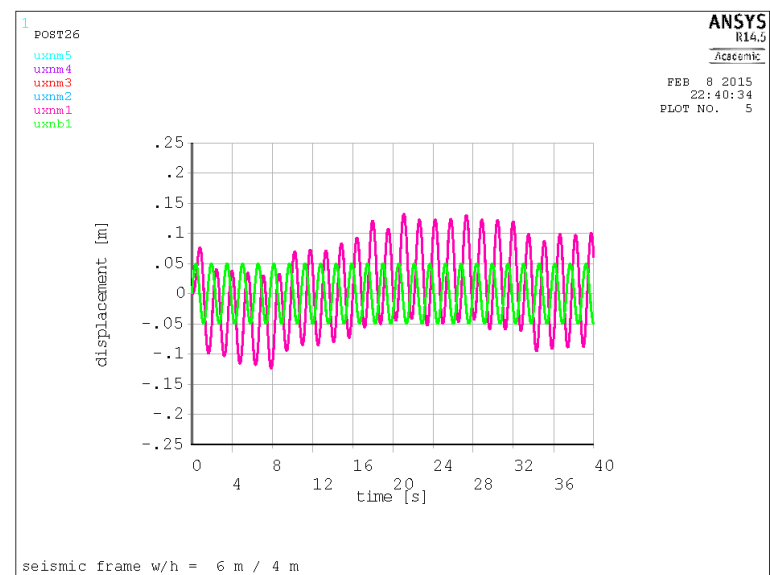
40 seconds with $1,635 \times 0,995$, EFAK = 5 and NINC = 200
(compare above run with NINC = 100, otherwise identical)
max at 39,2 sec -217 mm



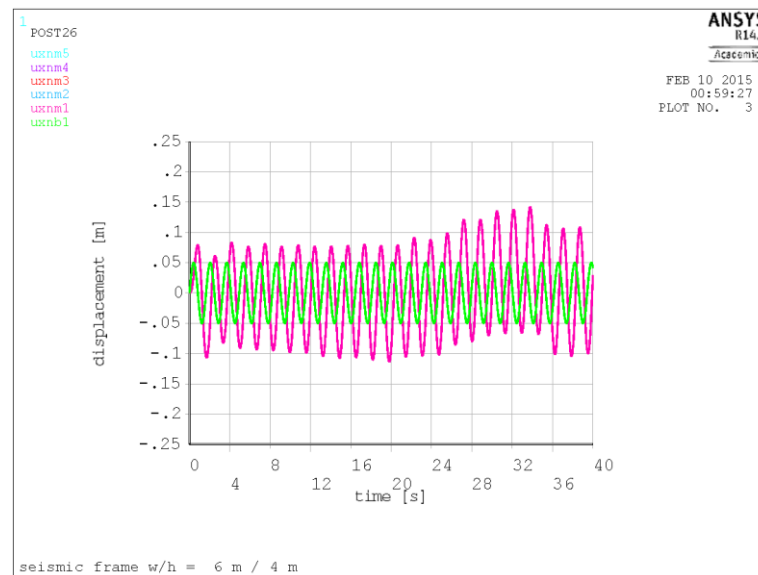
40 seconds with $1,635 \times 0,990$, EFAK = 5 and NINC = 200
max at 38,8 sec +213 mm



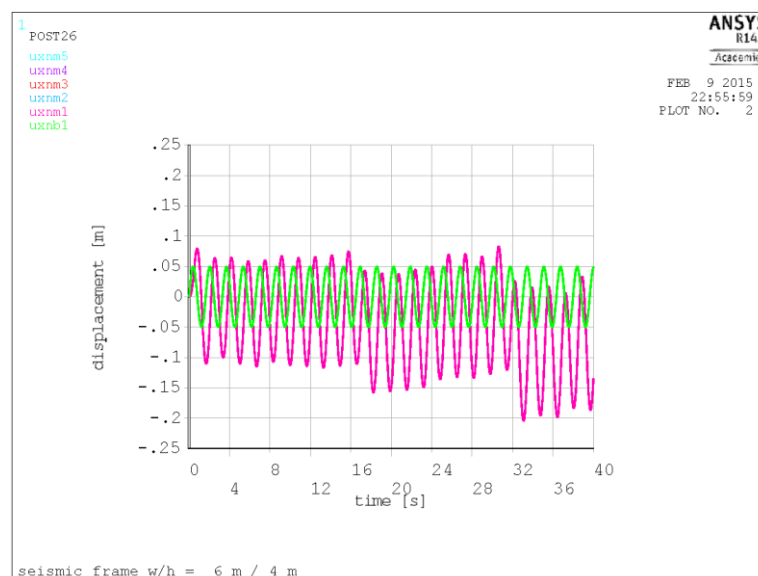
40 seconds with $1,635 \times 0,980$, EFAK = 5 and NINC = 200
max at 34,5 sec +150 mm



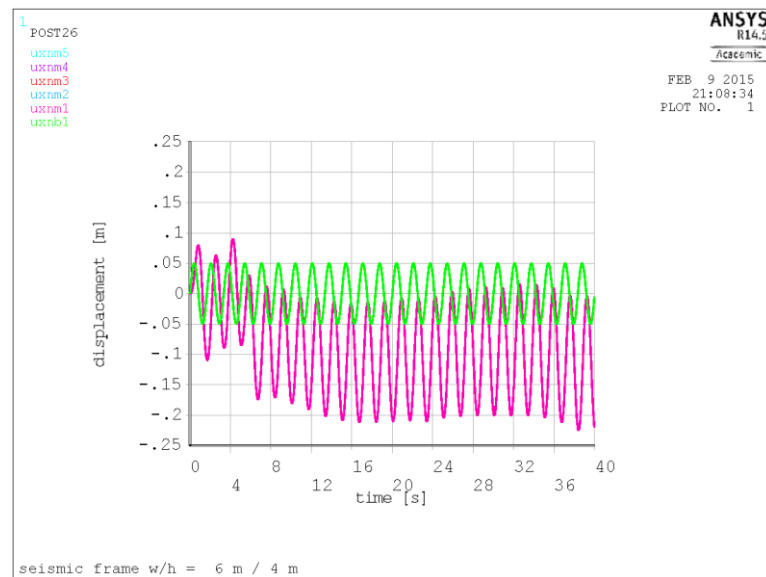
40 seconds with $1,635 \times 0,950$, EFAK = 5 and NINC = 200
max at 21,1 sec +132 mm



40 seconds with $1,635 \times 1,005$, EFAK = 5 and NINC = 200
max at 33,8 sec +142 mm

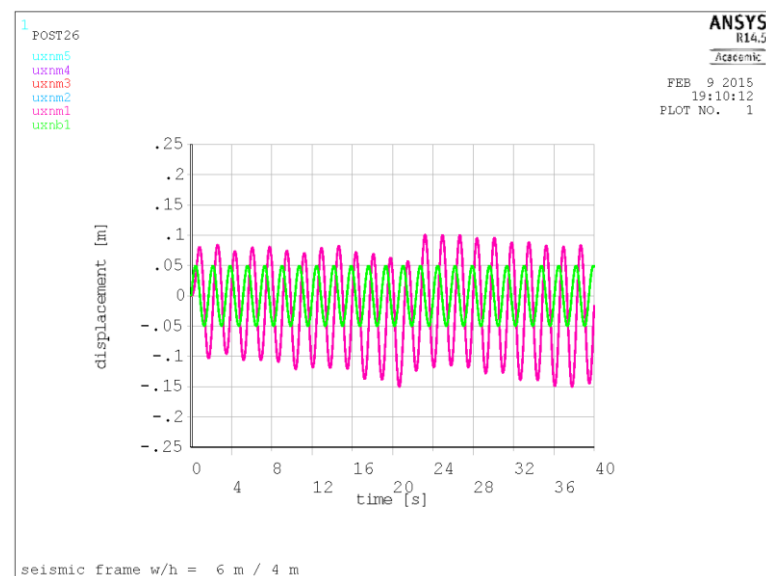


40 seconds with $1,635 \times 1,010$, EFAK = 5 and NINC = 200
max at 33,1 sec -204 mm



40 seconds with 1,635*1,020, EFAK = 5 and NINC = 200

max at 38,4 sec –225 mm



40 seconds with 1,635*1,050, EFAK = 5 and NINC = 200

max at 20,5 sec –150 mm

max at 36,1 sec –149 mm

max at 37,8 sec –150 mm

8 Open Questions

- What is a result?
see Model 1 – plastic “1,635*1,003”
is this going up forever?
which is the steady state?

9 References

- [1] Knoedel, P.: On the Dynamics of Steel Structures with X-Type Bracing. Stahlbau 80 (2011), No. 8, p. 566-571.
- [2] Knoedel, P., Hrabowski, J.: Seismic Design in Plant Construction – Shortcomings of EC8. In: Dunai, L., Ivany, M., Jarmai, K., Kovacs, N., Vigh, L.G. (eds.): Proceedings Vol. B, p. 1083–1988, Eurosteel 2011, 6th European Conference on Steel and Composite Structures, Budapest, Hungary, 31.08.-02.09.2011.
- [3] Knoedel, P., Hrabowski, J.: Yield Limit vs. Behaviour Factor in Seismic Design. Proceedings, NSCC 2012 Nordic Steel Construction Conference, 5-7 September 2012, Oslo, Norway, pp 147-155.
- [4] Knoedel, P., Hrabowski, J., Ummenhofer, T.: Seismic behaviour factor in combined frame and braced structures. EuroSteel 2014, 7th EUROpean conference on STEEL and Composite Structures, Naples, Italy, 10-12 September 2014.